

# Digital 3D printing of concrete structures using FEM

**Michaela Vaitová**

**Libor Jendele**

**Jan Červenka**

*Červenka Consulting Ltd., Praha*

## Content:

Digital printing of concrete

Implementation in ATENA

Material model for concrete

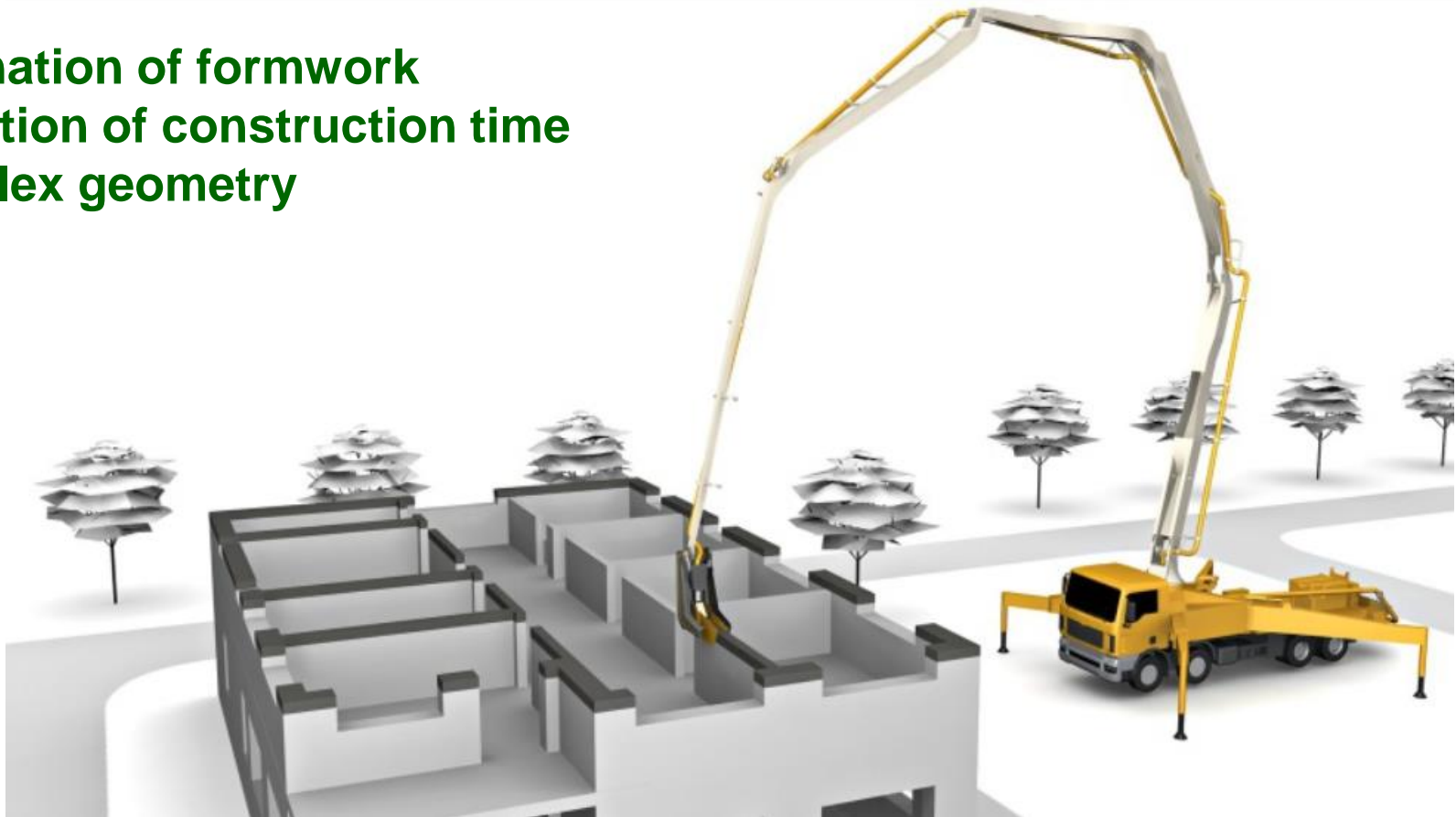
Validation

Sample analysis

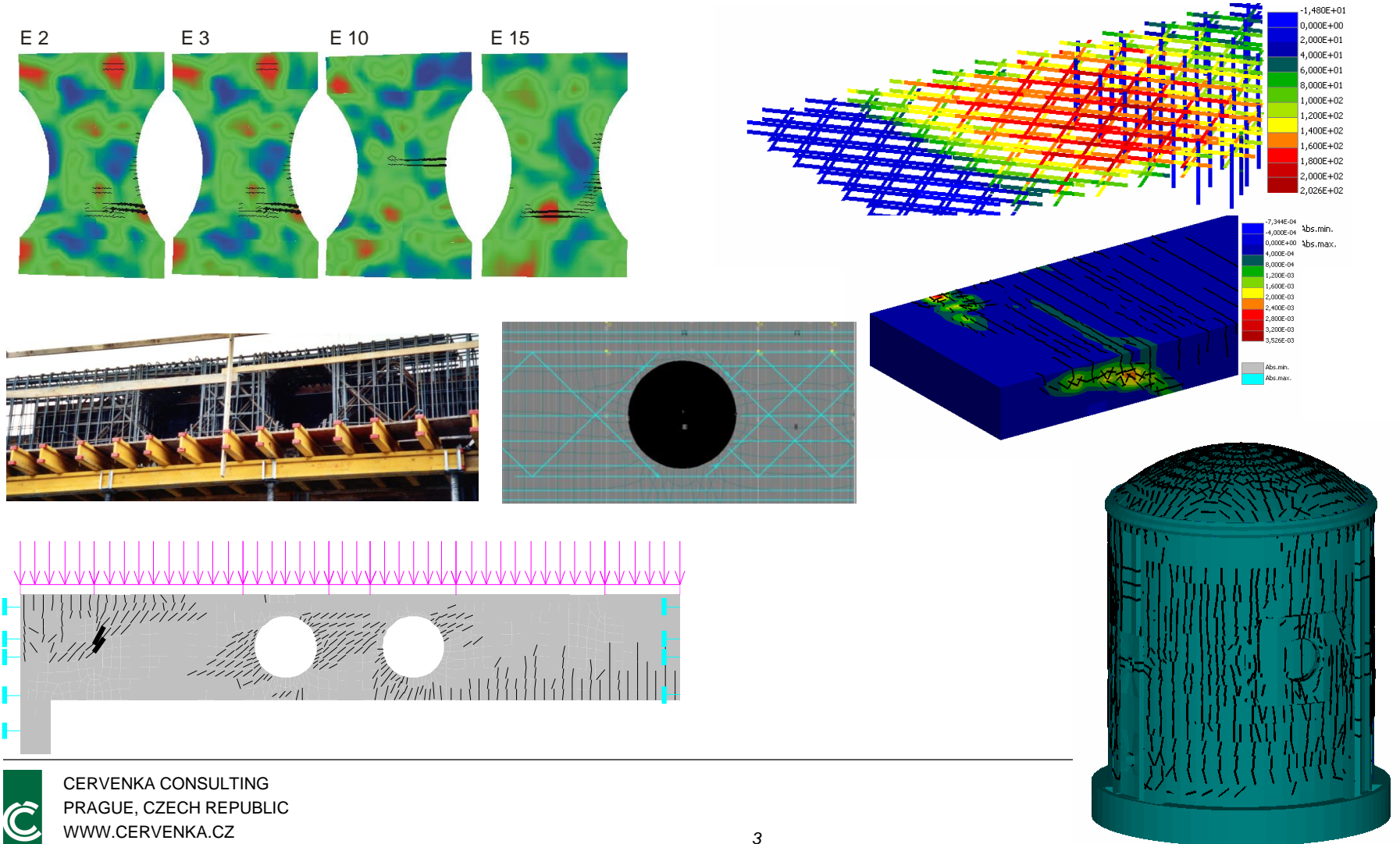


## Digital printing of concrete

- elimination of formwork
- reduction of construction time
- complex geometry



# Nonlinear simulation of reinforced concrete structures



## ATENA modelling of digital printing of concrete

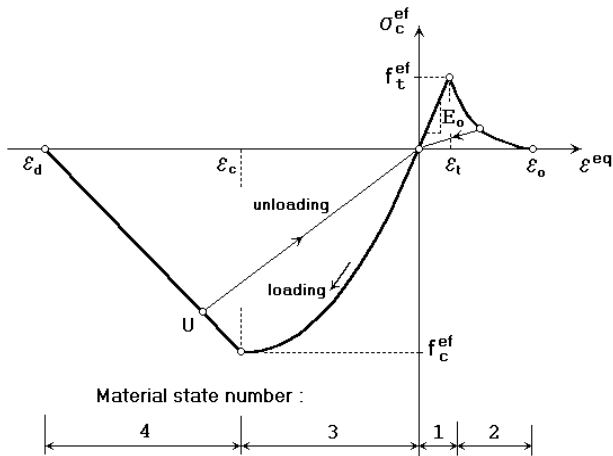
- material model developing in time
- construction process for model
- time effect on load: self weight, shrinkage
- visualization while running



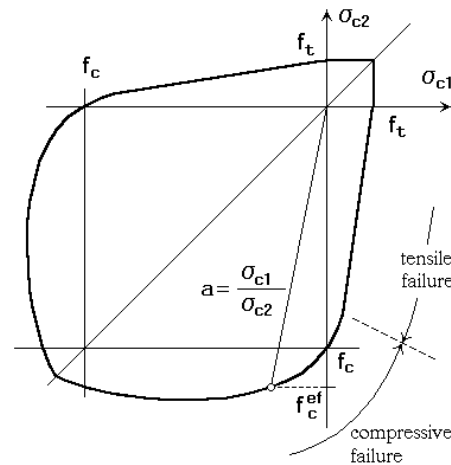
# Material model of concrete

## - fracture-plastic

Uniaxial law

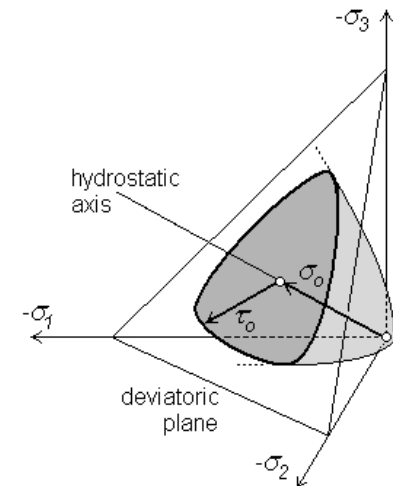


Bi-axial criterion



Kupfer 1969

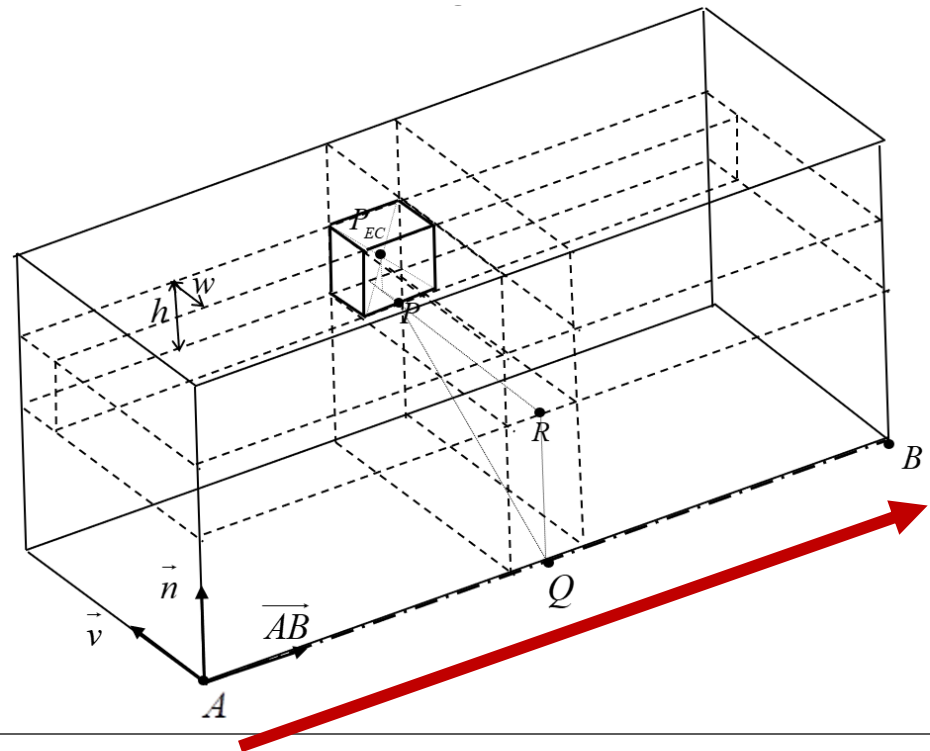
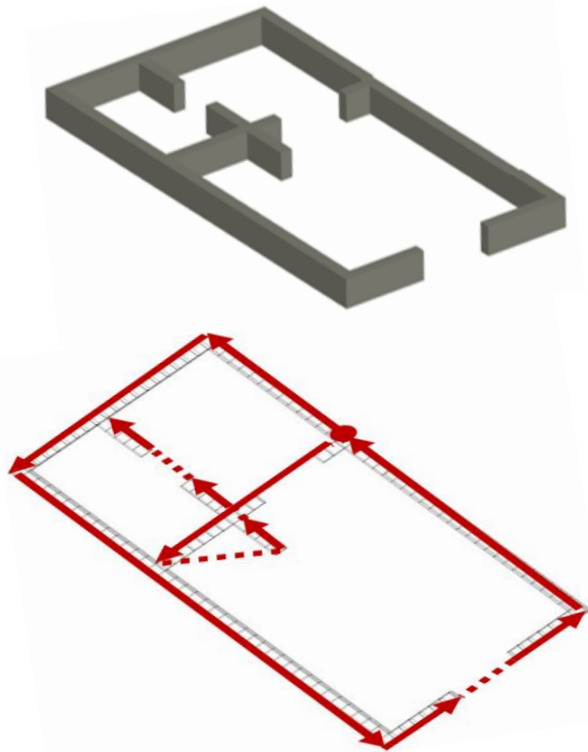
3D failure surface



Menetrey Willam, ACI 1995

## Construction process

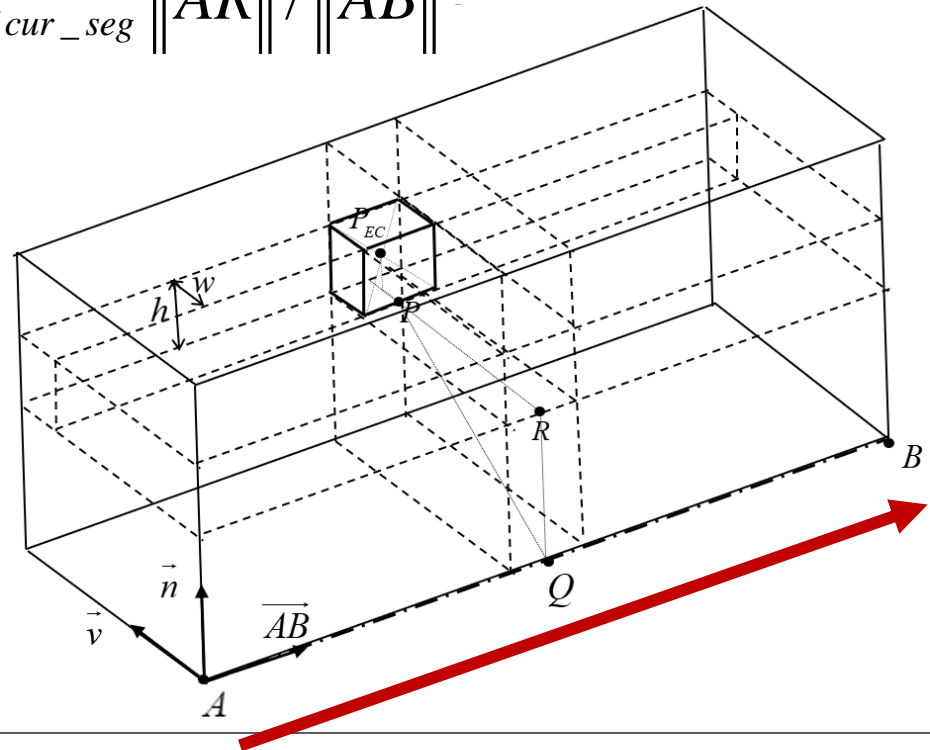
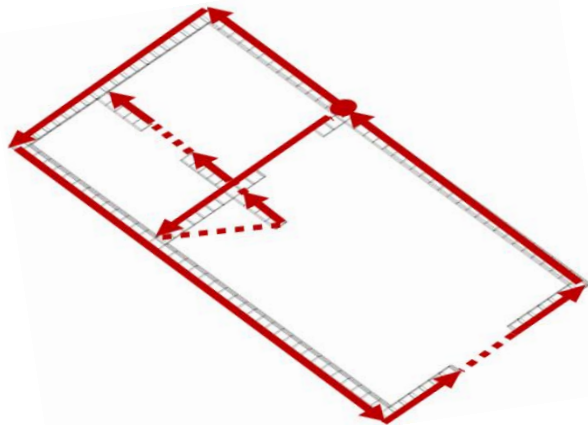
- determination of construction time for each element



## Construction process

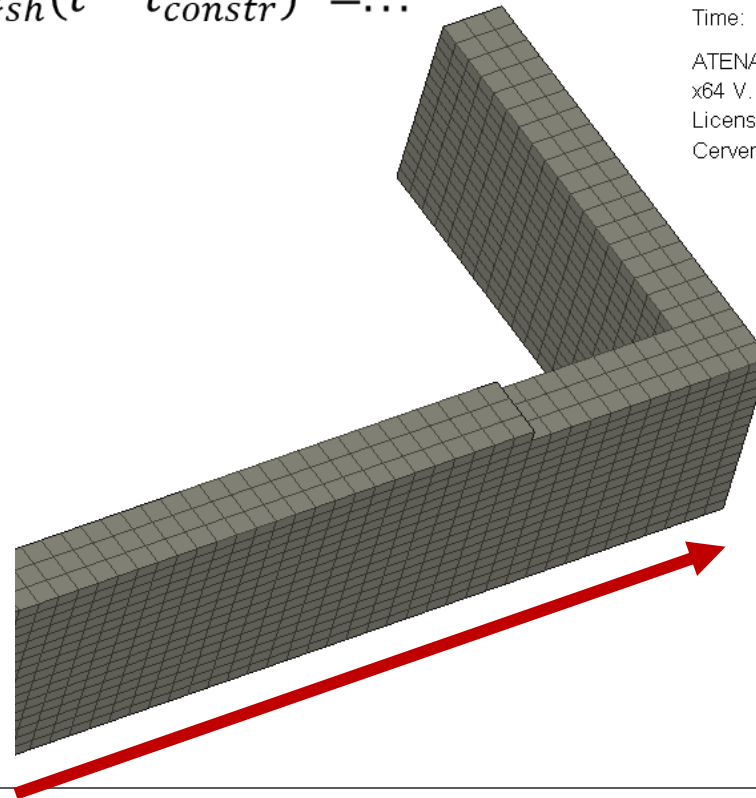
- determination of construction time for each element

$$t_i^{constr} = (l_{id} - 1) t_{layer} + t_{prev\_segs} + t_{cur\_seg} \left\| \frac{\overrightarrow{AR}}{\overrightarrow{AB}} \right\|$$



## Time effect on load

- self weight body load is applied while printing
- shrinkage element load  $\varepsilon_{sh}(t - t_{constr}) = \dots$

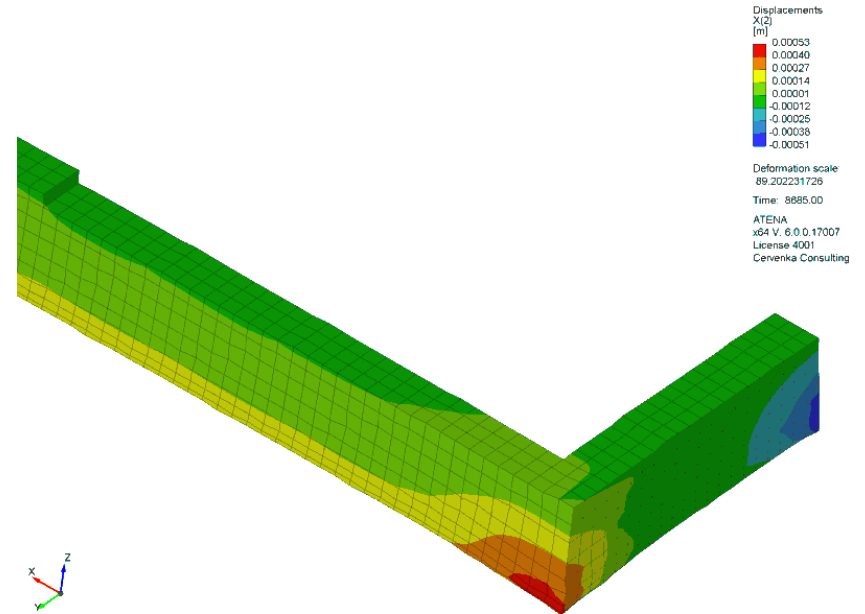
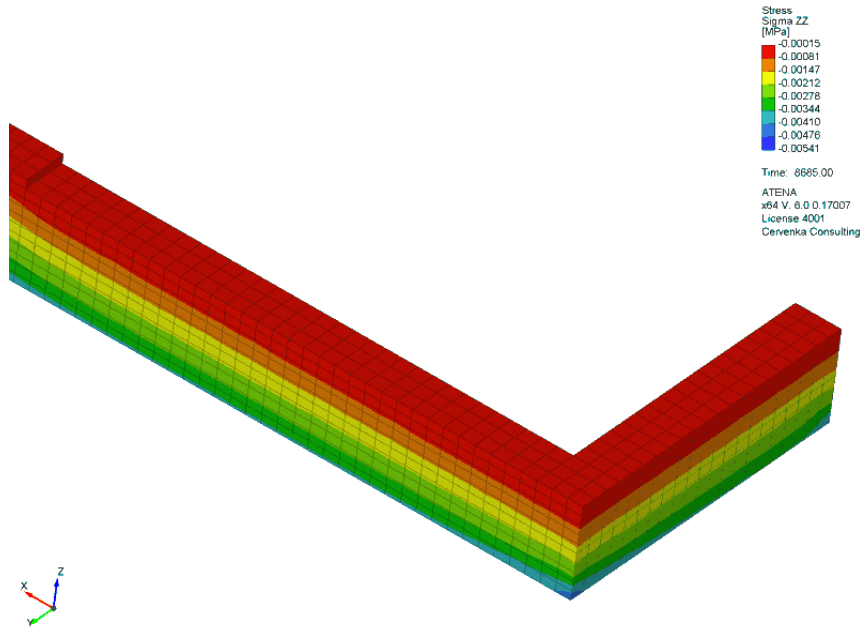


Time: 8250.00

ATENA  
x64 V. 6.0.0.1667E  
License 4001  
Cervenka Consultir

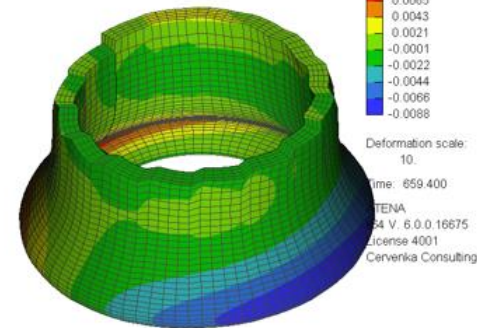
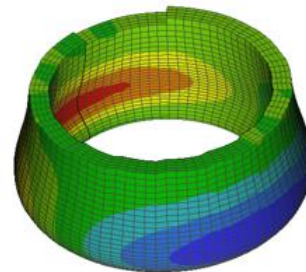
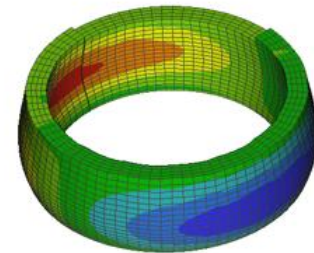
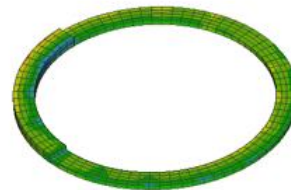
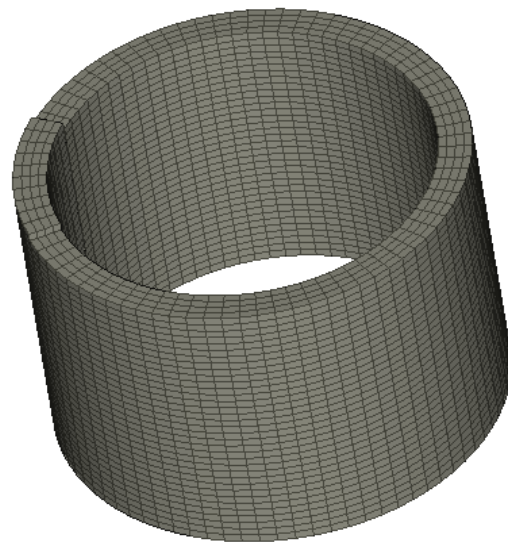


# Visualization



## Validation based on literature

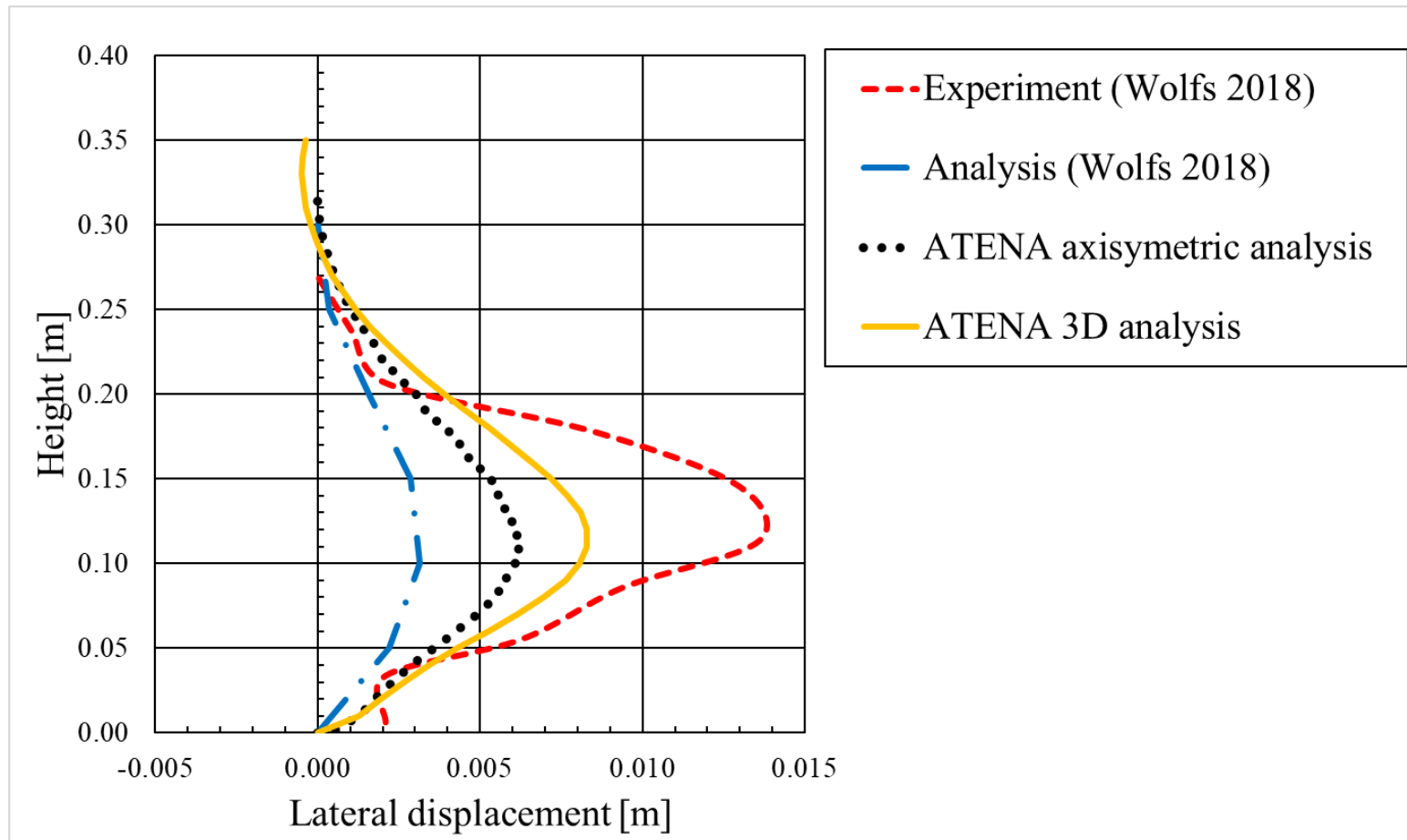
### Wolfs at.al. example:



## Wolfs at.al. material

Parameter	Name	Unit	Reference
Young modulus	$E$	MPa	Uniaxial compressive test
Poisson ratio	$\nu$	-	Uniaxial compressive test
Tensile strength	$f_t$	MPa	Direct shear test
Compressive strength	$f_c$	MPa	Uniaxial compressive test
Onset of nonlinear behavior in compression	$f_{c,0}$	MPa	Estimated
Specific fracture energy	$G_f$	kN/m	Model code
Critical compressive displacement	$\epsilon_{cp}$	m	Uniaxial compressive test (Force vs. displacement plot)
Plastic strain at compressive strength	$w_d$	-	Uniaxial compressive test (Stress vs. strain plot)
Specific weight	$\gamma$	kN/m <sup>3</sup>	weighting
Aggregate size	$a_g$	m	sieving

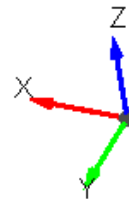
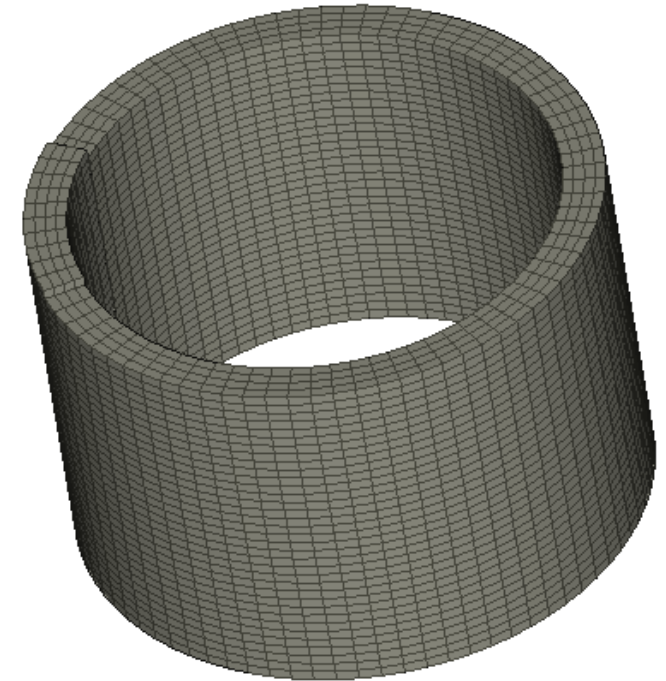
# Lateral displacement Experiment vs. Numerical models



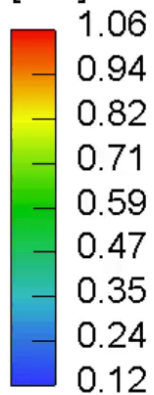
## Critical height Experiment vs. Numerical models

Wolfs at.al. example:

-Wolfs 3D experiment	0.29m
-Euler load	0.33m
-Wolfs axisym. (Abacus )	0.46m
-Atena axisym.	0.33m
-Atena 3D model	0.36m



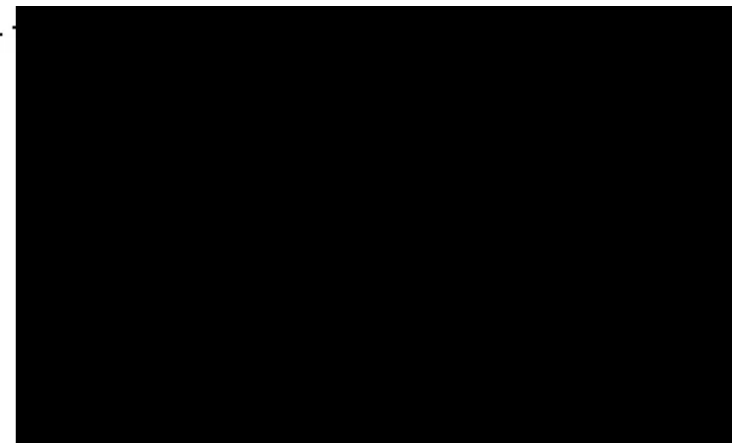
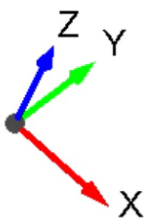
Element Constr  
Constr.T.  
[sec]



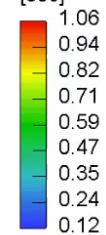
Deformation sca  
589.07707

Time: 1.17750

ATENA  
x64 V. 6.0.0.166  
License 4001  
Cervenka Consu



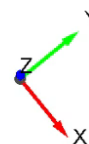
Element Constr  
Constr.T.  
[sec]



Deformation sca  
589.07707

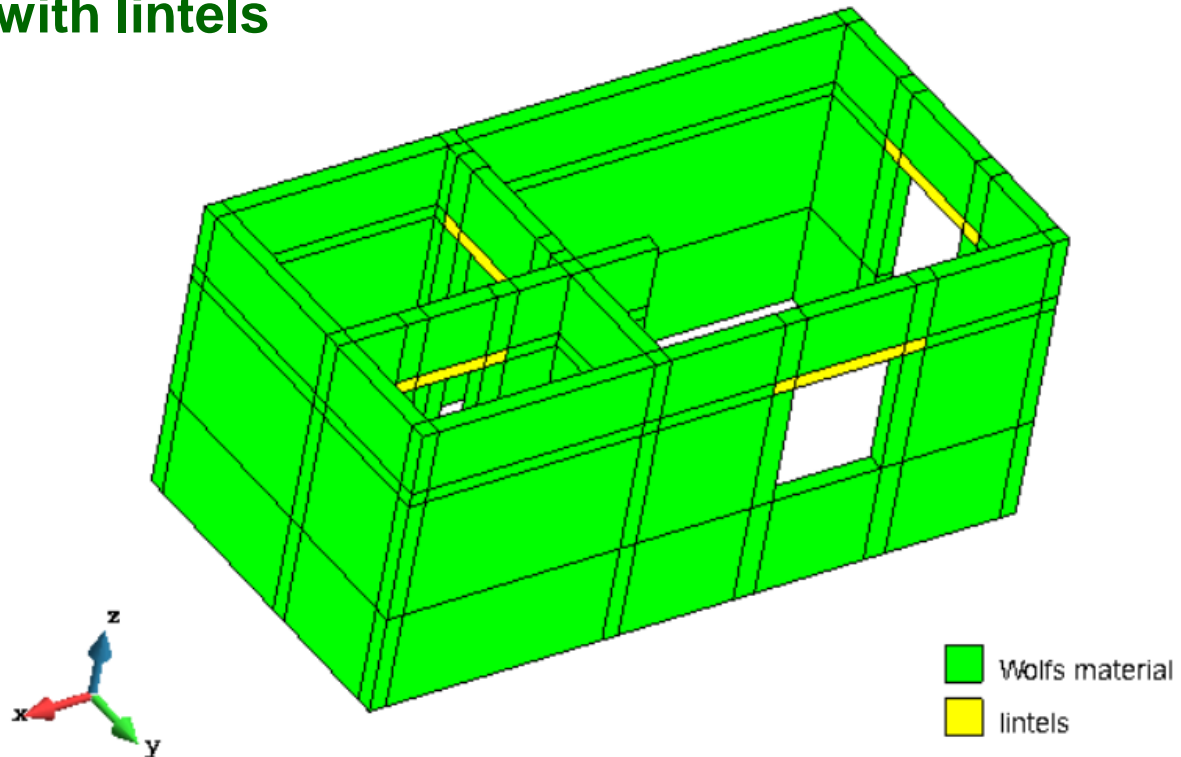
Time: 1.17750

ATENA  
x64 V. 6.0.0.166  
License 4001  
Cervenka Consu



## Sample analysis

- Simple house with lintels



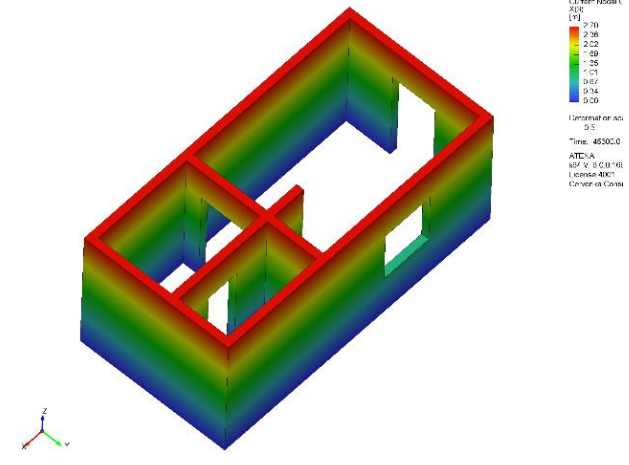
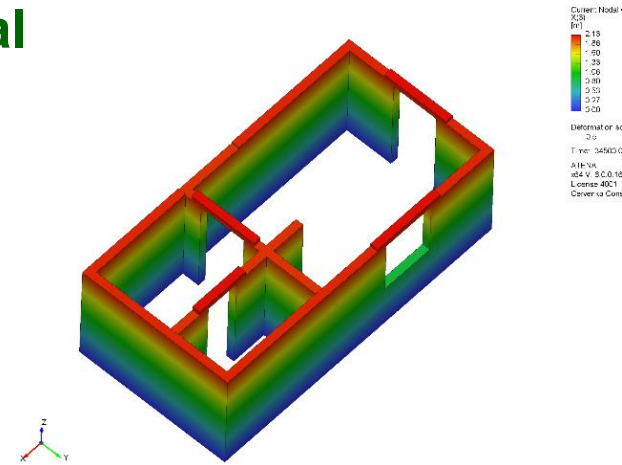
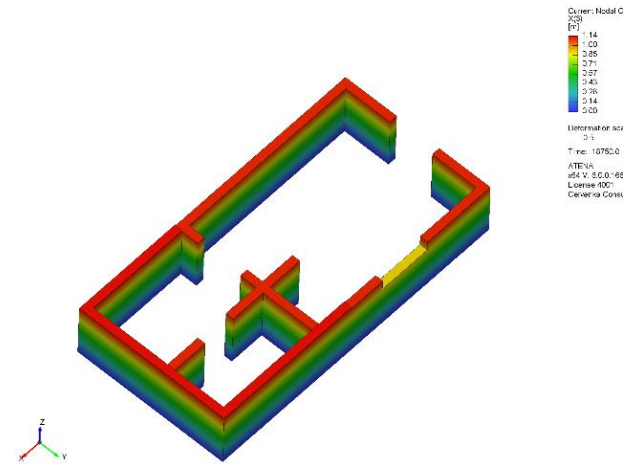
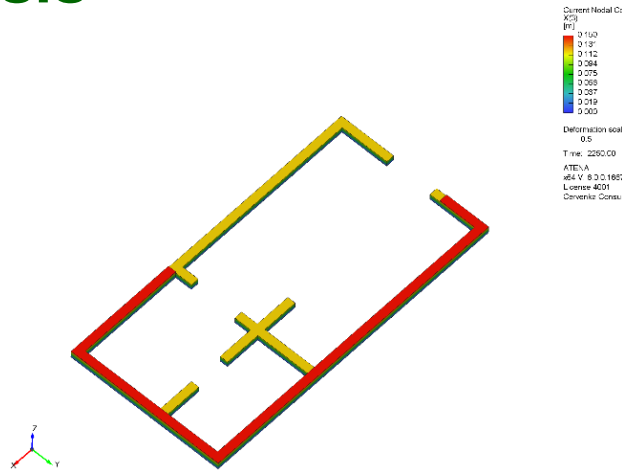
-Project digiCON2 – TU Dresden, Cerion, Cervenka Consulting s.r.o.

# Sample analysis

-Printing speed:  
5 cm/s

-Printed layer  $h$ :  
3 cm

-Maximum lateral  
displacement:  
4 mm



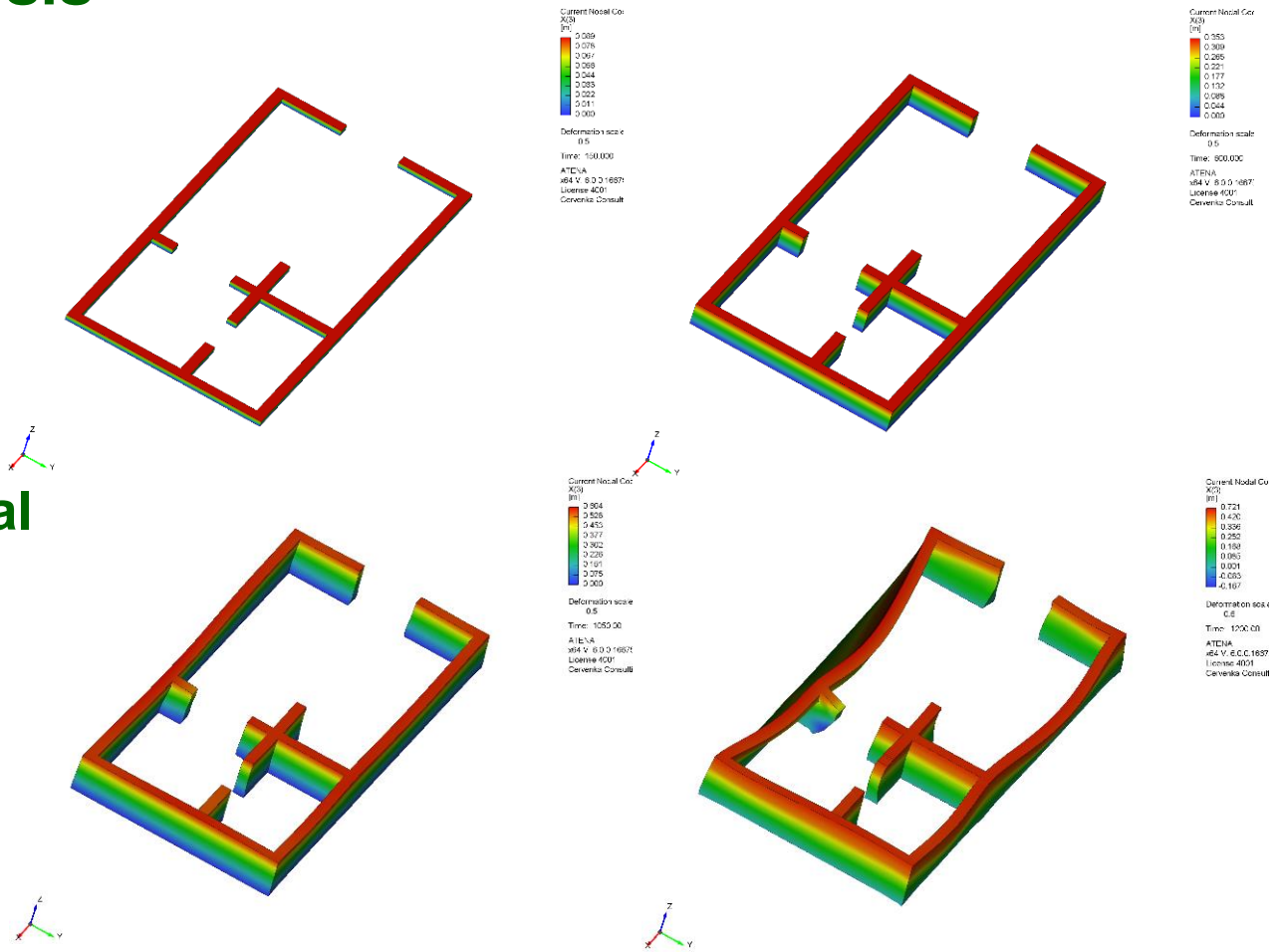


# Sample analysis

-Printing speed:  
50 cm/s

-Printed layer  $h$ :  
3 cm

-Maximum lateral  
displacement:  
0.9 m



## **Conclusions**

- ATENA module for digital printing of concrete as an extension of standard FEM**
- Simple implementation and use**
- Available for civil engineering practice**
- Good compromise between accuracy, user labor and CPU demands**
- Validation analyses – good accuracy**

## Aknowledgement

**TAČR TF04000051 DigiCon2 project "Software for simulation service for digital concrete production,, Technology Agency of Czech Rep.**

**T A  
Č R**

**THANK YOU  
FOR YOUR ATTENTION**

